Aligned to the 2014 Common Core Standards for Mathematics

ENGAGING STUDENTS • FOSTERING ACHIEVEMENT • CULTIVATING 21ST CENTURY GLOBAL SKILLS

Introduction

The State of New Jersey adopted the Common Core Standards for Mathematics in June of 2010 and requires implementation in grades K-12 beginning in September of 2012. The Wandell School mathematics curriculum for grades K-5 incorporates the State of New Jersey's model curriculum for mathematics.

Common Core Standards for Mathematics:

The K-5 standards provide students with a solid foundation in whole numbers, addition, subtraction, multiplication, division, fractions and decimals—which help young students build the foundation to successfully apply more demanding math concepts and procedures, and move into applications.

The standards stress not only procedural skill but also conceptual understanding, to make sure students are learning and absorbing the critical information they need to succeed at higher levels.

These standards define what students should understand and be able to do in their study of mathematics. What does mathematical understanding look like? One hallmark of mathematical understanding is the ability to justify, in a way appropriate to the student's mathematical maturity, why a particular mathematical statement is true or where a mathematical rule comes from. There is a world of difference between a student who can summon a mnemonic device to expand a product such as (a + b)(x + y) and a student who can explain where the mnemonic comes from. The student who can explain the rule understands the mathematics, and may have a better chance to succeed at a less familiar task such as expanding (a + b + c)(x + y). Mathematical understanding and procedural skill are equally important, and both are assessable using mathematical tasks of sufficient richness.

All students must have the opportunity to learn and meet the same high standards if they are to access the knowledge and skills necessary in their post-school lives. The standards do provide clear signposts along the way to the goal of college and career readiness for all students.

National Governors Association Center for Best Practices, Council of Chief State School Officers. "Common Core State Standards - Mathematics." National Governors Association Center for Best Practices, Council of Chief State School Officers, Washington D.C., 2010. Web. 20 June 2012. http://www.corestandards.org/the-standards/mathematics.

Aligned to the 2014 Common Core Standards for Mathematics

ENGAGING STUDENTS • FOSTERING ACHIEVEMENT • CULTIVATING 21ST CENTURY GLOBAL SKILLS

Unit 1 Overview

Content Area: Mathematics

Unit Title: Operations and Algebraic Thinking

Target Course/Grade Level: Grade 2

Unit Summary

In this unit students develop addition and subtraction strategies based on their developing sense of how numbers can be composed and decomposed and on the inverse relationship between addition and subtraction. Students learn to create arrays of up to 5 rows and 5 columns, then add these equal groups to find the total, setting the foundation for multiplication and area in grade 3.

Primary interdisciplinary connections: Reading, Language Arts, Science, Social Studies

21st century themes:

- Critical Thinking/Problem Solving
- Communication
- Collaboration

Unit Rationale

A firm grounding in the big picture of how operations with numbers interrelate and how they are vital tools in life can help students build the positive attitudes that will help them become confident, efficient, and effective problem-solvers (McConnell, 2011)

Algebraic thinking develops problem-solving skills. Students must analyze what they know and don't know about a problem, determine a method for finding solutions, and check results for accuracy. Algebra provides students with resources for dealing with real-world situations in a "systematic, analytic manner." (McConnell, 2011)

Recognizing, analyzing and constructing patterns helps to build a "strong foundation of algebra readiness", and is central to both art and science. (McConnell, 2011)

Learning Targets

Standards

- <u>2.OA.A.1</u> Use addition and subtraction within 100 to solve one- and two-step word problems involving situations of adding to, taking from, putting together, taking apart, and comparing, with unknowns in all positions, e.g., by using drawings and equations with a symbol for the unknown number to represent the problem.
- <u>2.OA.B.2</u> Fluently add and subtract within 20 using mental strategies. By the end of Grade 2, know from memory all sums of two one-digit numbers.
- <u>2.OA.C.4</u> Use addition to find the total number of objects arranged in rectangular arrays with up to 5 rows and up to 5 columns; write an equation to express the total as a sum of equal addends.
- <u>2.NBT.B.5</u> Fluently add and subtract within 100 using strategies based on place value, properties of operations, and/or the relationship between addition and subtraction.
- <u>2.NBT.B.6</u> Add up to four two-digit numbers using strategies based on place value and properties of operations.
- <u>2.NBT.B.9</u> Explain why addition and subtraction strategies work, using place value and the properties of operations.

Content Statements

• Represent and solve problems involving addition and subtraction.

Aligned to the 2014 Common Core Standards for Mathematics

ENGAGING STUDENTS • FOSTERING ACHIEVEMENT • CULTIVATING 21ST CENTURY GLOBAL SKILLS

- Add and subtract within 20.
- Work with equal groups of objects to gain foundations for multiplication.
- Use place value understanding and properties of operations to add and subtract.

CPI#	Cumulative Progress Indicator (CPI) from NJDOE Model Curriculum							
2.OA.A.1	Add and subtract within 100 to solve 1- and 2-step word problems with unknowns in any position.							
2.OA.B.2	• Add and subtract fluently within 20 using mental strategies such as decomposing and composing numbers using 10 as the benchmark number.							
	• By the end of grade 2, know from memory all sums of two 1-digit numbers.							
2.OA.C.4	Write an addition equation with repeated equal addends from a rectangular array (up to 5 rows and 5 columns) and solve to find the total number.							
2.NBT.B.5	Use a variety of strategies (place value, properties of operations, and/or the relationship between addition and subtraction) to add and subtract within 100.							
2.NBT.B.6	Add up to four 2-digit numbers based on place value and properties of operations.							
2.NBT.B.9	Apply addition and subtraction strategies based on place value and the properties of operations and explain why they work using drawings or objects.							

Unit Essential Questions

- Topic 1: What are some ways to think about addition and subtraction?
- Topic 2: What are strategies for finding addition facts?
- Topic 3: What are strategies for finding subtraction facts?
- Topic 4: What is the relationship between arrays and repeated addition?

Unit Enduring Understandings

Topic 1:

- *Parts of a whole* is one interpretation of addition. Addition number sentences can be used to show parts of a whole.
- *Joining parts to make a whole* is one interpretation of addition. Addition number sentences can be used to show *joining parts of a whole*.
- Separating parts from a whole and comparison are two interpretations of subtraction. Subtraction number sentences can be used to show separating parts from a whole or comparison subtraction situations
- Addition and subtraction have an inverse relationship. The inverse relationship between addition and subtraction can be used to find subtraction facts; every subtraction fact has a related addition fact.
- Some problems can be solved by using objects to act out the actions in the problem.

Topic 2:

- The number relationships of *0-more-than*, *1-more-than*, and *2-more-than* are the basis for addition facts with 0, 1, and 2.
- Doubles facts can be associated with memorable real-world situations.
- Basic addition facts that are near doubles can be found using a related doubles fact.

Aligned to the 2014 Common Core Standards for Mathematics

ENGAGING STUDENTS • FOSTERING ACHIEVEMENT • CULTIVATING 21ST CENTURY GLOBAL SKILLS

- Addition facts involving 9 can be changed to an equivalent fact with 10. Addition facts involving 8 can be changed to an equivalent fact with 10.
- Two numbers can be added in any order.
- Three or more numbers can be grouped and added in any order.
- Information in a problem can often be shown using a picture or diagram and used to understand and solve the problem. Some problems can be solved by writing and completing a number sentence or equation.

Topic 3:

- The number relationships of *0-less-than*, *1-less-than*, and *2-less-than* are the basis for subtraction facts with 0, 1, and 2.
- Addition and subtraction have an inverse relationship. The inverse relationship between addition and subtraction can be used to find subtraction facts; every subtraction fact has a related addition fact.
- Some subtraction facts can be found by subtracting from minuend (the larger number) an amount to get to 10 and then subtracting the amount that remains.
- Sometimes the answer to one problem or question is needed to find the answer to another problem or question.

Topic 4:

- Repeated addition involves joining equal groups.
- An array involves joining equal groups and is one way to think about repeated addition.
- Information in a problem can often be shown using a diagram and used to solve the problem.
 Some problems can be solved by writing and completing a number sentence or equation.

Unit Learning Targets

Students will ...

- add and subtract within 100 to solve 1- and 2-step word problems with unknowns in any position.
- add up to four 2-digit numbers using place value and properties of operations.
- understand that numbers can be added in any order.
- understand that numbers can be grouped in any order, then added.
- add and subtract fluently within 20 mentally using 10 as a benchmark.
- use a variety of strategies to add and subtract within 100.
- write an addition equation with repeated equal addends from a rectangular array of up to 5 rows and 5 columns, then solve to find the total number.

Aligned to the 2014 Common Core Standards for Mathematics

ENGAGING STUDENTS • FOSTERING ACHIEVEMENT • CULTIVATING 21ST CENTURY GLOBAL SKILLS

- apply addition and subtraction strategies based on place value and properties of operations, then explain why they work using drawings or objects.
- know from memory all sums of two 1-digit numbers by the end of Grade 2.

Evidence of Learning

Summative Assessment (14 days per topic)

Each topic has a summative test and performance assessment.

Materials needed: listed in each topic as per teacher's guide for that topic.

Teacher Resources:

enVision Math Common Core: Realize Edition Topic 1, Understanding Addition and Subtraction

enVision Math Common Core: Realize Edition Topic 2, Addition Strategies enVision Math Common Core: Realize Edition Topic 3, Subtraction Strategies enVision Math Common Core: Realize Edition Topic 4, Working with Equal Groups

Formative Assessments

• teacher observation

homework

• Lesson Additional Activity

• prior knowledge assessment

guided practice

• Lesson Quick Check

• Daily Common Core Review

Topic/Lesson Plans									
Topic	Timeframe								
Topic 1	14 days								
Understanding Addition and Subtraction	14 days								
Topic 2	14 days								
Addition Strategies									
Topic 3	14 days								
Subtraction Strategies	14 days								
Topic 4	1.4 dove								
Working with Equal Groups	14 days								

Teacher Notes:

This unit consists of four topics from the *enVision Math Common Core* series with anywhere from 4 to 7 lessons per topic. These four topics address the Operations and Algebraic Thinking domain of the Common Core Standards for Mathematics for Grade 2 students. In addition, these four topics address all eight of the Standards for Mathematical Practice.

Essential questions and enduring understandings were taken directly from the textbook series used by the district, *enVision Math Common Core: Realize Edition*

Curriculum Development Resources

Click the links below to access additional resources used to design this unit:

NJDOE. "Model Curriculum: Mathematics (K-12) - Grade 2." *Model Curriculum: Mathematics (K-12) - Grade 2*. New Jersey Dept. of Education, n.d. Web. 08 Apr. 2015. http://www.state.nj.us/education/modelcurriculum/math/1.shtml.

Aligned to the 2014 Common Core Standards for Mathematics

ENGAGING STUDENTS • FOSTERING ACHIEVEMENT • CULTIVATING 21ST CENTURY GLOBAL SKILLS

Charles, Randall. *enVision Math Common Core*. Realize ed. Grade 1. Upper Saddle River: Pearson Education, 2015. Print. enVision Math Common Core

"Grade 2 » Operations & Algebraic Thinking." Grade 2 » Operations & Algebraic Thinking. N.p., n.d. Web. 08 Apr. 2015. http://www.corestandards.org/Math/Content/1/OA/

Aligned to the 2014 Common Core Standards for Mathematics

ENGAGING STUDENTS • FOSTERING ACHIEVEMENT • CULTIVATING 21ST CENTURY GLOBAL SKILLS

Topic 1														
Content Area: Mathematics														
Topic	Topic Title: Understanding Addition and Subtraction Timeframe: 14 days													
	Lesson Components													
	21st Century Themes													
	obal vareness	X	Financi Busines Entrepr	ss, and			Civic Literac	су		Health Literacy	7		Environ Literacy	mental
					<u>21</u> ^s	st C	entury	Skil	ls					
	reativity ar	nd	X		cal Thinkin lem Solving		nd	X	Coı	mmunicat	ion	X	Coll	aboration
		rv (Connect		cience, Soc		Studies	Read	ding	Language	e Arts			
					l resources						• 11105,			
_	rials need			B			1							
• n	umber cub	es												
• c	ounters													
• C	onnecting o	cub	es											
• p	aper bag													
• n														
• p	aper													
• c	rayons													
• p	art-part-wh	ole	mat											
• ir	ndex cards													
	vo-color co													
Topic	c 1 Vocabu	ılar	y:											
_	art													
	hole													
• a	dd													
	um													
	addition sentence													
_	plus (+)													
	equals (=)													
-	oin													
	ubtract													
	ifference													
	ubtraction s	sent	ence											
	ninus (-)													
	eparate													
• n	nore													

Aligned to the 2014 Common Core Standards for Mathematics

ENGAGING STUDENTS • FOSTERING ACHIEVEMENT • CULTIVATING 21ST CENTURY GLOBAL SKILLS

- fewer
- related
- fact family

Goals/Objectives	Learning Activities/Instructional Strategies	Formative Assessment Tasks
 Students: will join two groups and write addition number sentences to tell how many in all. (1-1) will model joining stories and write an addition number sentence. (1-2) will solve problems by writing subtraction number sentences. (1-3) will write subtraction sentences to solve stories about separating groups. (1-4) will write subtraction sentences to solve stories about comparing groups. (1-5) will write related addition and subtraction facts. (1-6) will use counters to model and solve addition and subtraction problems. (1-7) 	1. Interactive Math Story 2. Topic Opener: game and vocabulary introduction 3. Daily Common Core Review 4. Problem-Based Interactive Learning Activity 5. Develop the Concept: Visual Learning a. Guided Practice b. Independent Practice and Problem Solving 6. Close/Assess and Differentiate a. lesson Quick Check b. prescribe differentiated instruction c. assess leveled homework	 guided practice Do You Understand? question lesson Quick Check differentiated activities/worksheets leveled homework

Differentiation

- TE pg. 1E
- embedded within each lesson
- differentiated worksheets/activities for each lesson
- leveled homework for each lesson
- reteaching resources at the end of each lesson

Resources Provided

• enVision Math Common Core: Realize Edition Topic 1 - 4 teacher's guides, workbooks, digital

Aligned to the 2014 Common Core Standards for Mathematics

ENGAGING STUDENTS • FOSTERING ACHIEVEMENT • CULTIVATING 21ST CENTURY GLOBAL SKILLS

resources, manipulatives		

Topic 2										
Content Area: Mathema	tics									
Topic Title: Addition Stra	tegies		Timefr	ame: 14 days						
Lesson Components										
	21st Century Themes									
Awareness Busin	cial, Economic, ess, and preneurial Literacy	Civic Literacy	Health Literacy	Environmental Literacy						
	21 st C	Century Skil	<u>lls</u>							
Creativity and Innovation	x Critical Thinking an Problem Solving	nd x	Communication	x Collaboration						
Interdisciplinary Connec	ctions: Science, Social	Studies, Read	ding, Language Arts	5,						
Integration of Technolog	y: digital resources are	part of this s	eries							

Materials needed:

- counters
- paper clips
- pencils
- number cards 0-11
- connecting cubes
- paper bags
- crayons
- beads
- index cards
- double ten-frame mat
- two-color counters
- number cubes
- cotton balls

Topic 2 Vocabulary:

- doubles
- near doubles
- addend
- number sentence

Aligned to the 2014 Common Core Standards for Mathematics

ENGAGING STUDENTS • FOSTERING ACHIEVEMENT • CULTIVATING 21ST CENTURY GLOBAL SKILLS

Goals/Objectives	Learning Activities/Instructional Strategies	Formative Assessment Tasks
 will master addition facts involving 0, 1, and 2. (2-1) will master addition facts in which both addends are the same. (2-2) will master addition facts where the addends are 1 apart. (2-3) will use the commutative property to find sums. (2-4) will find the sum of three addends using any order. (2-5) will find sums by making 10 when adding. (2-6) will draw a picture and write a number sentence to solve a story problem. (2-7) 	 Lesson Sequence Interactive Math Story Topic Opener: game and vocabulary introduction Daily Common Core Review Problem-Based Interactive Learning Activity Develop the Concept: Visual Learning Guided Practice Independent Practice and Problem Solving Close/Assess and Differentiate lesson Quick Check prescribe differentiated instruction assess leveled homework 	 guided practice Do You Understand? question lesson Quick Check differentiated activities/worksheets leveled homework

Differentiation

- TE pg. 35C
- embedded within each lesson
- differentiated worksheets/activities for each lesson
- leveled homework for each lesson
- reteaching resources at the end of each lesson

Resources Provided

• enVision Math Common Core: Realize Edition Topic 1 – 4 teacher's guides, workbooks, digital resources, manipulatives

Aligned to the 2014 Common Core Standards for Mathematics

ENGAGING STUDENTS • FOSTERING ACHIEVEMENT • CULTIVATING 21ST CENTURY GLOBAL SKILLS

	Topic 3													
(Content Area: Mathematics													
T	Topic Title: Subtraction StrategiesTimeframe: 14 days													
	Lesson Components													
	21st Century Themes													
	Global Awareness	X	Busir	ies	al, Economic, s, and eneurial Literacy		Civic Literac	:y	Health Literacy			Environmental Literacy		
					<u>21st</u>	C	entury	Ski	lls					
	Creativity ar Innovation	nd		X	Critical Thinking and Problem Solving			X	Communication				X	Collaboration
I	nterdisciplina	ry (Conne	cti	ons: Science, Soci	al S	Studies,	Read	ding,	Langı	age Art	s,		
I	ntegration of T	Гес	hnolog	gy:	digital resources a	are	part of t	his s	series					
N	• counters	car	ds 0-1	1 a	and 12-20									
	• connect	_												
	paper arnumber	•												
	• subtract			ard	S									
	• two-cole													
	• cups													
	 double t 	en-	frame	ma	nt									
T	opic 3 Vocabu		•											
	• no new	voc	cabular	у	words									

Goals/Objectives	Learning Activities/Instructional Strategies	Formative Assessment Tasks
Students: • will subtract 0, 1, and 2 from a number by applying the concepts of <i>0-less-than</i> , <i>1-less-than</i> , and <i>2-less-than</i> a number. (3-1) • will use addition doubles facts to	 Lesson Sequence Interactive Math Story Topic Opener: game and vocabulary introduction Daily Common Core Review Problem-Based Interactive Learning Activity Develop the Concept: Visual Learning 	 guided practice Do You Understand? question lesson Quick Check differentiated activities/worksheets leveled homework

Aligned to the 2014 Common Core Standards for Mathematics

ENGAGING STUDENTS • FOSTERING ACHIEVEMENT • CULTIVATING 21ST CENTURY GLOBAL SKILLS

subtract. (3-2)	a. Guided Practice	
 will find differences by 	b. Independent Practice and Problem	
using related addition	Solving	
facts to 10. (3-3)	6. Close/Assess and Differentiate	
 will find differences by 	a. lesson Quick Check	
using related addition	b. prescribe differentiated instruction	
facts to 18. (3-4)	c. assess leveled homework	
• will use the <i>make-10</i>		
strategy to subtract.		
(3-5)		
 will solve two-question 		
problems by using the		
answer to the first		
question to answer the		
second question. (3-6)		

Differentiation

- TE pg. 69C
- embedded within each lesson
- differentiated worksheets/activities for each lesson
- leveled homework for each lesson
- reteaching resources at the end of each lesson

Resources Provided

• enVision Math Common Core: Realize Edition Topic 1 – 4 teacher's guides, workbooks, digital resources, manipulatives

	Topic 4											
C	Content Area: Mathematics											
To	Topic Title: Working with Equal Groups Timeframe: 14 days											
	Lesson Components											
	21st Century Themes											
	Global Awareness	X	Busin	ncial, Economic, ness, and epreneurial Literacy			Civic Literac	у		Health Literacy		nvironmental teracy
	21st Century Skills											
				Critical Thinking Problem Solving		d	X	Com	munication	X	Collaboration	

Aligned to the 2014 Common Core Standards for Mathematics

ENGAGING STUDENTS • FOSTERING ACHIEVEMENT • CULTIVATING 21ST CENTURY GLOBAL SKILLS

Interdisciplinary Connections: Science, Social Studies, Reading, Language Arts,

Integration of Technology: digital resources are part of this series

Materials needed:

- counters
- paper clips
- pencils
- two-color counters
- crayons
- index cards

Topic 4 Vocabulary:

array

Goals/Objectives	Learning Activities/Instructional Strategies	Formative Assessment Tasks				
 Students: will model repeated addition to write number sentences. (4-1) will build arrays to model repeated addition situations. (4-2) will use repeated addition to solve problems. (4-3) will draw pictures and write number sentences to solve addition problems. (4-4) 	 Lesson Sequence Interactive Math Story Topic Opener: game and vocabulary introduction Daily Common Core Review Problem-Based Interactive Learning Activity Develop the Concept: Visual Learning Guided Practice Independent Practice and Problem Solving Close/Assess and Differentiate lesson Quick Check prescribe differentiated instruction c. assess leveled homework 	 guided practice Do You Understand? question lesson Quick Check differentiated activities/worksheets leveled homework 				

Differentiation

- TE pg. 99C
- embedded within each lesson
- differentiated worksheets/activities for each lesson
- leveled homework for each lesson
- reteaching resources at the end of each lesson

Aligned to the 2014 Common Core Standards for Mathematics

ENGAGING STUDENTS • FOSTERING ACHIEVEMENT • CULTIVATING 21ST CENTURY GLOBAL SKILLS

Resources Provided

• enVision Math Common Core: Realize Edition Topic 1 – 4 teacher's guides, workbooks, digital resources, manipulatives

Unit 2 Overview

Content Area: Mathematics

Unit Title: Number and Operations in Base Ten

Target Course/Grade Level: Grade 2

Unit Summary

This unit involves students in making sense of our number system by continuing their experiences with counting numbers. Counting experiences provide children with an exposure to place value which is the basis of the structure of our number system. Students use connecting cubes to model numbers; the cubes give students opportunities to observe the combinations of tens and ones needed to create a given number and to compose and decompose tens when adding two numbers. Children use a hundreds chart to observe patterns in the number system. These experiences strengthen students' number sense and form the foundation for success in problem solving. Students are taught to use place value to develop mental addition and subtraction strategies. The focus is on understanding the structure of numbers to add and subtract, rather than arbitrary rules. By the end of the unit, students are adding and subtracting within 1,000 using strategies based on place-value understanding, properties of operations, and the relationship of addition and subtraction as inverse operations. Throughout the unit, students apply their number sense to solve one- and two-step word problems.

Primary interdisciplinary connections: Reading, Language Arts, Science, Social Studies

21st century themes:

- Critical Thinking/Problem Solving
- Communication
- Collaboration

Unit Rationale

A firm grounding in the big picture of how operations with numbers interrelate and how they are vital tools in life can help students build the positive attitudes that will help them become confident, efficient, and effective problem-solvers (McConnell, 2011)

Algebraic thinking develops problem-solving skills. Students must analyze what they know and don't know about a problem, determine a method for finding solutions, and check results for accuracy. Algebra provides students with resources for dealing with real-world situations in a "systematic, analytic manner." (McConnell, 2011)

Recognizing, analyzing and constructing patterns helps to build a "strong foundation of algebra readiness", and is central to both art and science. (McConnell, 2011)

Learning Targets

Aligned to the 2014 Common Core Standards for Mathematics

ENGAGING STUDENTS • FOSTERING ACHIEVEMENT • CULTIVATING 21ST CENTURY GLOBAL SKILLS

Standards

- 2.NBT.A.1a 100 can be thought of as a bundle of ten tens called a "hundred."
- <u>2.NBT.A.1b</u> The numbers 100, 200, 300, 400, 500, 600, 700, 800, 900 refer to one, two, three, four, five, six, seven, eight, or nine hundreds (and 0 tens and 0 ones).
- 2.NBT.A.2 Count within 1000; skip-count by 5s, 10s, and 100s
- <u>2.NBT.A.3</u> Read and write numbers to 1000 using base-ten numerals, number names, and expanded form.
- <u>2.NBT.A.4</u> Compare two three-digit numbers based on meanings of the hundreds, tens, and ones digits, using >, =, and < symbols to record the results of comparisons.
- <u>2.NBT.B.5</u> Fluently add and subtract within 100 using strategies based on place value, properties of operations, and/or the relationship between addition and subtraction.
- <u>2.NBT.B.6</u> Add up to four two-digit numbers using strategies based on place value and properties of operations.
- <u>2.NBT.B.8</u> Mentally add 10 or 100 to a given number 100-900, and mentally subtract 10 or 100 from a given number 100-900
- <u>2.NBT.B.7</u> Add and subtract within 1000, using concrete models or drawings and strategies based on place value, properties of operations, and/or the relationship between addition and subtraction; relate the strategy to a written method. Understand that in adding or subtracting three-digit numbers, one adds or subtracts hundreds and hundreds, tens and tens, ones and ones; and sometimes it is necessary to compose or decompose tens or hundreds.
- <u>2.NBT.B.9</u> Explain why addition and subtraction strategies work, using place value and the properties of operations.
- <u>2.OA.A.1</u> Use addition and subtraction within 100 to solve one- and two-step word problems involving situations of adding to, taking from, putting together, taking apart, and comparing, with unknowns in all positions, e.g., by using drawings and equations with a symbol for the unknown number to represent the problem.
- <u>2.OA.C.3</u> Determine whether a group of objects (up to 20) has an odd or even number of members, e.g., by pairing objects or counting them by 2s; write an equation to express an even number as a sum of two equal addends.
- <u>2.MD.B.6</u> Represent whole numbers as lengths from 0 on a number line diagram with equally spaced points corresponding to the numbers 0, 1, 2, ..., and represent whole-number sums and differences within 100 on a number line diagram.

Content Statements

- Understand place value.
- Understand that the three digits of a three-digit number represent amounts of hundreds, tens, and ones; e.g., 706 equals 7 hundreds, 0 tens, and 6 ones.
- Use place value understanding and properties of operations to add and subtract.
- Represent and solve problems involving addition and subtraction.
- Work with equal groups of objects to gain foundations for multiplication.
- Relate addition and subtraction to length.

CPI#	Cumulative Progress Indicator (CPI) from NJDOE Model Curriculum
2.NBT.A.1a	Represent a 3-digit number as specific amounts of 100s, 10s, and 1s.
	Identify 10 tens as 100

Aligned to the 2014 Common Core Standards for Mathematics

ENGAGING STUDENTS • FOSTERING ACHIEVEMENT • CULTIVATING 21ST CENTURY GLOBAL SKILLS

2.NBT.A.1b	Represent the century numbers as a 2, 3, 4,9 followed by two zeros to indicate no tens and no ones.
2.NBT.A.2	Skip count by 5s, 10s, and 100s to 1000 beginning at any multiple of 1, 5, 10, or 100.
2.NBT.A.3	 Read numbers to 1,000 using base-ten numerals, number names and expanded form. Write numbers to 1,000 using base-ten numerals, number names and expanded form.
2.NBT.A.4	Use <, >, and = to record the results of comparing two 3-digit number by decomposing the 3-digit number into 100s, 10s, and 1s.
2.NBT.B.5	Use a variety of strategies (place value, properties of operations, and/or the relationship between addition and subtraction) to fluently add and subtract within 100.
2.NBT.B.6	Add up to four 2-digit numbers based on place value and properties of operations.
2.NBT.B.7	Add and subtract within 1000, using concrete models or drawings and strategies based on place value, properties of operations, and/or the relationship between addition and subtraction; relate the strategy to a written method. Understand that in adding or subtracting three-digit numbers, one adds or subtracts hundreds and hundreds, tens and tens, ones and ones; and sometimes it is necessary to compose or decompose tens or hundreds.
2.NBT.B.8	Apply properties of place value to mentally add or subtract 10 or 100 to/from a given number within 100-900.
2.NBT.B.9	Apply addition and subtraction strategies based on place value and the properties of operations and explain why they work using drawings or objects.
2.OA.A.1	Add and subtract within 100 to solve 1- and 2-step word problems with unknowns in any position.
2.OA.C.3	 Recognize that in groups of even numbers, objects can be counted by 2s, and that in groups of odd numbers, objects will not pair up evenly (one will be left over). Write an equation to illustrate that all even numbers can be formed from the addition of two equal addends.,
2.MD.B.6	Use a number line of equally spaced points to represent whole number sums and differences (within 100) related to length
2.MD.B.6	

Unit Essential Questions

- Topic 5: How can numbers to 100 be shown and compared?
- Topic 6: How can sums be found mentally?
- Topic 7: How can differences be found mentally?
- Topic 8: What is a standard procedure for adding two-digit numbers?
- Topic 9: What is a standard procedure for subtracting two-digit numbers?
- Topic 10: What number patterns are helpful I reading and writing numbers to 1,000?
- Topic 11: What are the ways to add and subtract three-digit numbers?

Unit Enduring Understandings Topic 5:

- In a two-digit number, the tens digit tells how many groups of ten and the ones digit tells the number of ones.
- The numbers 21-99 are written by joining two number words that describe the number of tens and the number of ones. Numbers through 20 are each represented by a unique number word.
- Our place value number system makes it easy to name the number that is 10 more or 10 less than any other given number by simply adjusting the digit in the tens place.
- Numbers can be used to tell how many.
- Place value can be used to compare and order

Aligned to the 2014 Common Core Standards for Mathematics

ENGAGING STUDENTS • FOSTERING ACHIEVEMENT • CULTIVATING 21ST CENTURY GLOBAL SKILLS

numbers

- The position words *before* and *after* can be used to explain number relationships.
- Some numbers can be divided into equal parts (even numbers) and some cannot (odd numbers).
- In order to solve some problems, data need to be selected from a source outside the statement of the problem, like a chart.

Topic 6:

- Adding tens is like adding ones.
- When adding a number less than ten to a twodigit number using the traditional algorithm, it may be necessary to rename 10 ones as 1 ten.
- Two-digit numbers can be broken apart using tens and ones and added in different ways.
- Patterns on a hundred chart can be used to add numbers and to develop mental math strategies and number sense.
- Adding groups of tens is similar to adding numbers less than ten.
- Some problems can be solved by identifying elements that repeat in a predictable way.

Topic 7:

- Subtracting tens is like subtracting ones.
- To find parts of 100, add on ones to make a ten and count on by tens to reach 100.
- Patterns in a hundred chart can be used to subtract numbers and to develop mental math strategies and number sense.
- Subtracting groups of tens is similar to subtracting numbers less than ten.
- Some problems have data missing needed to find the answer, and some problems have extra data not needed to solve the problem.

Topic 8:

- 10 ones can be regrouped for 1 ten.
- The standard addition algorithm for two-digit and one-digit numbers breaks the calculation into simpler calculations using place value, starting with the ones and then the tens.
 Answers to the simpler calculations are used to give the final sum.
- The standard algorithm for adding two-digit and two-digit numbers is just an extension of the algorithm for adding two-digit and one-digit

Aligned to the 2014 Common Core Standards for Mathematics

ENGAGING STUDENTS • FOSTERING ACHIEVEMENT • CULTIVATING 21ST CENTURY GLOBAL SKILLS

- numbers. The ones are added first, and then the tens
- All sums and differences can be found using models (cubes). Some calculations are done easily using mental math or paper and pencil. More complex calculations can be done using a calculator.
- Sums can be represented as lengths on a number line diagram of addition.
- Three and four two-digit numbers can be grouped and added in any order.
- Information in a problem can often be shown using a diagram to solve the problem. Some problems can be solved by writing and completing a number sentence or equation.

Topic 9:

- 1 ten can be regrouped for 10 ones.
- The standard subtraction algorithm breaks the calculation into simpler calculations starting with the ones and then the tens.
- The standard algorithm for subtracting two-digit and two-digit numbers is just an extension of the algorithm for subtracting two-digit and one-digit numbers.
- All sums and differences can be found using models (cubes). Some calculations are done easily using mental math or paper and pencil. More complex calculations can be done using a calculator.
- Differences can be represented as lengths in a number line diagram of subtraction.
- The inverse relationship between addition and subtraction can be used to check subtraction.
- Sometimes the answer to one problem/question is needed to find the answer to another problem/question.

Topic 10:

- Numbers can be used to tell how many.
- Our number system is based on groups of ten.
 Whenever we get 10 in one place value, we move to the next greater place value.
- Adding or subtracting hundreds or tens is similar to adding or subtracting single-digit numbers.
- Counting and place-value patterns can be seen on a hundreds chart.

Aligned to the 2014 Common Core Standards for Mathematics

ENGAGING STUDENTS • FOSTERING ACHIEVEMENT • CULTIVATING 21ST CENTURY GLOBAL SKILLS

- Number lines can help with skip counting.
- Place value can be used to compare and order numbers.
- Some problems can be solved by identifying elements that repeat in a predictable way.

Topic 11:

- There are a variety of ways to add three-digit numbers.
- There is more than one way to do a mental calculation. Techniques for doing addition or subtraction calculations mentally involve changing the numbers or the expressions so the calculation is easy to do mentally.
- There is more than one way to estimate a sum. Rounding gives one way to estimate sums.
- The standard addition algorithm for three-digit numbers breaks the calculation into simpler calculations using place value starting with the ones, then the tens, and then the hundreds.
- There is a variety of ways to subtract three-digit numbers.
- The standard subtraction algorithm for threedigit numbers breaks the calculation into simpler calculations using place value starting with the ones, then the tens, and then the hundreds.
- Some problems can be solved by reasoning about the conditions in the problem.

Unit Learning Targets

Students will be able to . .

- represent a number as specific amounts of 100s, 10s, and 1s.
- identify 10 tens as 100.
- Represent the century numbers as a 2, 3, 4, . . 9 indicating the number of hundreds, followed by two zeros, representing no tens and no ones.
- Skip count by 5s and 10s to 100.
- Read and write numbers to 1,000 using base-ten numerals, number names, and expanded form.
- Use symbols <, >, and = to record the results of comparing two 3-digit numbers by decomposing the number into 100s, 10s and 1s.
- Add up to four 2-digit numbers using strategies based on place value and properties of operations.
- Count within 1,000 by 1s, 5s, 10s, and 100s beginning at any multiple of 1, 5, 10 or 100.
- apply a variety of strategies to add and subtract within 1000.
- Apply properties of place value to mentally add or subtract 10 or 100 from a given number within 100-900.
- Explain why a chosen addition or subtraction strategy works with drawings or objects.

Aligned to the 2014 Common Core Standards for Mathematics

ENGAGING STUDENTS • FOSTERING ACHIEVEMENT • CULTIVATING 21ST CENTURY GLOBAL SKILLS

- Understand that when adding and subtracting it may be necessary to compose or decompose tens or hundreds.
- Add and subtract 1- and 2-step word problems within 100 with unknowns in any position.
- Recognize that objects in groups of even numbers can be counted by 2s and objects in groups of odd numbers will not pair up evenly.
- Write an equation to illustrate that all even numbers can be formed from the addition of two equal addends.
- Use a number line to represent whole number sums and differences related to length within 100 by using equally spaced points.

Evidence of Learning

Summative Assessment (14 days per topic)

Each topic has a summative test and performance assessment.

Materials needed: listed in each topic as per teacher's guide for that topic.

Teacher Resources:

enVision Math Common Core: Realize Edition Topic 5, Place Value to 100

enVision Math Common Core: Realize Edition Topic 6, Mental Addition

enVision Math Common Core: Realize Edition Topic 7, Mental Subtraction

enVision Math Common Core: Realize Edition Topic 8, Adding Two-Digit Numbers

enVision Math Common Core: Realize Edition Topic 9, Subtracting Two-Digit Numbers

enVision Math Common Core: Realize Edition Topic 10, Place Value to 1,000

enVision Math Common Core: Realize Edition Topic 11, Three-Digit Addition and Subtraction

Formative Assessments

• teacher observation

homework

• Lesson Additional Activity

- prior knowledge assessment
- guided practice
- Lesson Quick Check
- Daily Common Core Review

Topic/Lesson Plans									
Topic	Timeframe								
Topic 5	14 days								
Place Value to 100	14 days								
Topic 6	14 days								
Mental Addition	11 days								
Topic 7	14 days								
Mental Subtraction	17 days								
Topic 8	14 days								
Adding Two-Digit Numbers	14 days								
Topic 9	14 days								
Subtracting Two-Digit Numbers	14 days								
Topic 10	14 days								
Place Value to 1,000	17 days								
Topic 11	14 days								
Three-Digit Addition and Subtraction	14 days								

Aligned to the 2014 Common Core Standards for Mathematics

ENGAGING STUDENTS • FOSTERING ACHIEVEMENT • CULTIVATING 21ST CENTURY GLOBAL SKILLS

Teacher Notes:

This unit consists of seven topics from the *enVision Math Common Core* series with anywhere from 5 to 11 lessons per topic. These seven topics address the Number and Operations – Base Ten domain of the Common Core Standards for Mathematics for Grade 2 students. In addition, these four topics address all eight of the Standards for Mathematical Practice.

Essential questions and enduring understandings were taken directly from the textbook series used by the district, *enVision Math Common Core: Realize Edition*

Curriculum Development Resources

Click the links below to access additional resources used to design this unit:

NJDOE. "Model Curriculum: Mathematics (K-12) - Grade 2." *Model Curriculum: Mathematics (K-12) - Grade 2*. New Jersey Dept. of Education, n.d. Web. 08 Apr. 2015. http://www.state.nj.us/education/modelcurriculum/math/1.shtml.

Charles, Randall. *enVision Math Common Core*. Realize ed. Grade 1. Upper Saddle River: Pearson Education, 2015. Print. enVision Math Common Core

"Grade 2 » Number and Operations – Base Ten" Grade 2 » Number and Operations – Base Ten. N.p., n.d. Web. 10 Apr. 2015. http://www.corestandards.org/Math/Content/1/OA/

Common Core Standards Writing Team. (2011, May 29). Progressions for the Common Core State Standards in Mathematics (draft). *K, Counting and Cardinality; K–5, Operations and Algebraic Thinking*. Tucson, AZ: Institute for Mathematics and Education, University of Arizona.

Topic 5									
Content Area: Mathematics									
Topic Title: Place Value to 100					Timefr	ame	: 14 days		
Lesson Components									
21st Century Themes									
Global x Financial, Economic, Business, and Entrepreneurial Literac	y	Civic Literacy			Health Literacy		Environmental Literacy		
<u>2</u>	1 st C	entury	Skil	ls					
Creativity and x Critical Think Innovation Problem Solvi	_	nd	X	Communication		X	Collaboration		
Interdisciplinary Connections: Science,	ocial S	Studies,	Reac	ling,	Language Arts	5,			
Integration of Technology: digital resource	es are	part of t	his s	eries					

Aligned to the 2014 Common Core Standards for Mathematics

ENGAGING STUDENTS • FOSTERING ACHIEVEMENT • CULTIVATING 21ST CENTURY GLOBAL SKILLS

Materials needed:

- number cube 1-3
- game markers
- tens rods
- ones units
- connecting cubes
- number cards 0-11
- place value mat A
- index cards
- marker
- hundred chart
- sticky note
- crayons

Topic 5 Vocabulary:

- digits
- number word
- > (greater than)
- < (less than)
- = (equal to)
- before
- after
- even
- odd

Goals/Objectives	Learning Activities/Instructional Strategies	Formative Assessment Tasks			
 Students: will group objects into tens and ones to show two-digit numbers. (5-1) will read and write number words for numbers 0-99. (5-2) will compare two-digit numbers using symbols. (5-3) will identify and write numbers that are one before and one after given numbers. They 	 Lesson Sequence Interactive Math Story Topic Opener: game and vocabulary introduction Daily Common Core Review Problem-Based Interactive Learning Activity Develop the Concept: Visual Learning Guided Practice Independent Practice and Problem Solving Close/Assess and Differentiate lesson Quick Check 	 guided practice Do You Understand? question lesson Quick Check differentiated activities/worksheets leveled homework 			

Aligned to the 2014 Common Core Standards for Mathematics

ENGAGING STUDENTS • FOSTERING ACHIEVEMENT • CULTIVATING 21ST CENTURY GLOBAL SKILLS

will also count on and count back to identify missing numbers to 100. (5-4) b. prescribe differentiated instruction c. assess leveled homework	count back to identify missing numbers to 100.	*	
	numbers that are 10 more and 10 less than		
numbers that are 10 more and 10 less than	even and odd numbers.		
numbers that are 10 more and 10 less than given numbers. (5-5) • will learn to identify even and odd numbers.	chart to solve problems.		

Differentiation

- TE pg. 121C
- embedded within each lesson
- differentiated worksheets/activities for each lesson
- leveled homework for each lesson
- reteaching resources at the end of each lesson

Resources Provided

• enVision Math Common Core: Realize Edition Topic 5-11 teacher's guides, workbooks, digital resources, manipulatives

Topic 6										
Content Area: Mathematics										
Topic Title: Mental Addition Timeframe: 14 days									14 days	
Lesson Components										
21st Century Themes										
Awareness Bus	nes	al, Economic, s, and eneurial Literacy		Civic Literacy			Health Literacy		Environmental Literacy	
		21 st	C	entury	Skil	lls				
Creativity and x Critical Thinking Innovation Problem Solving				d	X	x Communicat			X	Collaboration
Interdisciplinary Conn	Interdisciplinary Connections: Science, Social Studies, Reading, Language Arts,									
Integration of Technolo	gy:	digital resources a	re	part of the	his s	eries				

Aligned to the 2014 Common Core Standards for Mathematics

ENGAGING STUDENTS • FOSTERING ACHIEVEMENT • CULTIVATING 21ST CENTURY GLOBAL SKILLS

Materials needed:

- counters
- number cards 0-11 and 12-20
- place value blocks
- paper bags
- index cards
- single ten-frame mat
- double ten-frame mat
- two-color counters
- little ten-frames
- hundred chart
- crayons
- connecting cubes

Topic 6 Vocabulary:

- mental math
- tens digit
- next ten

TE pg. 155C

embedded within each lesson

Goals/Objectives	Learning Activities/Instructional Strategies	Formative Assessment Tasks
 will mentally add multiples of 10 to a two-digit number. (6-1) will mentally add a two-digit number and a one-digit number. (6-2) will add a two-digit number to a two-digit number using mental math. (6-3) will use a hundred chart to add two 2-digit numbers. (6-4) will add using multiples of 10. (6-5) will use number patterns to solve problems. (6-6) 	 Lesson Sequence Interactive Math Story Topic Opener: game and vocabulary introduction Daily Common Core Review Problem-Based Interactive Learning Activity Develop the Concept: Visual Learning a. Guided Practice b. Independent Practice and Problem Solving Close/Assess and Differentiate a. lesson Quick Check b. prescribe differentiated instruction c. assess leveled homework 	 guided practice Do You Understand? question lesson Quick Check differentiated activities/worksheets leveled homework
Differentiation		

Aligned to the 2014 Common Core Standards for Mathematics

ENGAGING STUDENTS • FOSTERING ACHIEVEMENT • CULTIVATING 21ST CENTURY GLOBAL SKILLS

- differentiated worksheets/activities for each lesson
- leveled homework for each lesson
- reteaching resources at the end of each lesson

Resources Provided

• enVision Math Common Core: Realize Edition Topic 5-11 teacher's guides, workbooks, digital resources, manipulatives

		Topic 7	,						
Topic 7 Content Area: Mathematics									
Topic Title: Mental Subtraction					Timefr	am	e: 1	14 days	
	son	Compo	onent	s	11111011	••••		r days	
		ntury 1							
Global x Financial, Economic, Business, and Entrepreneurial Literacy	Civic Literacy			Health Literacy		Environmental Literacy			
<u>21</u> °	t C	entury	Skills	3					
Creativity and Innovation x Critical Thinking Problem Solving		ıd	x	Communication			X	Collaboration	
Interdisciplinary Connections: Science, Soc	ial S	Studies,	Readi	ng,	Language Arts	5,			
Integration of Technology: digital resources	are	part of t	his se	ries					
Materials needed:									
• game markers									
• number cards 0-9									
• counters									
• little ten-frames									
• crayons									
• hundred chart									
• place value blocks									
paperpencils									
connecting cubes									
Topic 7 Vocabulary:									
no new vocabulary									

Aligned to the 2014 Common Core Standards for Mathematics

ENGAGING STUDENTS • FOSTERING ACHIEVEMENT • CULTIVATING 21ST CENTURY GLOBAL SKILLS

Goals/Objectives	Learning Activities/Instructional Strategies	Formative Assessment Tasks
 Students: will subtract multiples of 10 from two-digit numbers using mental math. (7-1) will find the missing part of 100 by counting up from the given part. (7-2) will find the difference between two-digit numbers less than 100. (7-3) will explore different strategies to subtract two-digit numbers. (7-4) will determine whether they can solve problems with missing information or extra information. (7-5) 	 Lesson Sequence Interactive Math Story Topic Opener: game and vocabulary introduction Daily Common Core Review Problem-Based Interactive Learning Activity Develop the Concept: Visual Learning Guided Practice Independent Practice and Problem Solving Close/Assess and Differentiate lesson Quick Check prescribe differentiated instruction assess leveled homework 	 guided practice Do You Understand? question lesson Quick Check differentiated activities/worksheets leveled homework

Differentiation

- TE pg. 185C
- embedded within each lesson
- differentiated worksheets/activities for each lesson
- leveled homework for each lesson
- reteaching resources at the end of each lesson

Resources Provided

• enVision Math Common Core: Realize Edition Topic 5-11 teacher's guides, workbooks, digital resources, manipulatives

Topic 8								
Content Area: Mathematics								
Topic Title: Adding Two-Digit Numbers	Timeframe: 14 days							

Aligned to the 2014 Common Core Standards for Mathematics

ENGAGING STUDENTS • FOSTERING ACHIEVEMENT • CULTIVATING 21ST CENTURY GLOBAL SKILLS

Lesson Components												
21st Century Themes												
	Global Awareness	x Financial, Economic, Business, and Entrepreneurial Literacy				Civic Literacy			Health Literacy		Environmental Literacy	
					<u>21st</u>	C	entury	Skill	S			
	Creativity ar Innovation	nd		X	Critical Thinking Problem Solving		d	X	Cor	nmunication	X	Collaboration
Ir	nterdisciplina	ry (Conne	ctio	ons: Science, Soci	al S	Studies,	Read	ing,	Language Arts	s, Art	
Ir	ntegration of T	Гес	hnolog	gy:	digital resources a	ire	part of t	his se	eries			
M	laterials need	ed:										
	 unit cub 	es										
	 pencils 											
	 paper cl 	ips										
	 place va 	lue	mat A	1								
	• number	car	ds 0-1	1								
	• connect	ing	cubes									
	 colored 	•										
	 index ca 	ırds										
	• tape											
	• number											
T	opic 8 Vocabu	ılaı	·y:									
	 regroup 											
	• number line											

Goals/Objectives	Learning Activities/Instructional Strategies	Formative Assessment Tasks
 Students: will use models to add a one-digit number to a two-digit number. (8-1) will use concrete models to add a one-digit number to a two-digit number and decide if regrouping is needed. (8-2) will add a one-digit number to a two-digit number, regroup if necessary, and record 	 Lesson Sequence Interactive Math Story Topic Opener: game and vocabulary introduction Daily Common Core Review Problem-Based Interactive Learning Activity Develop the Concept: Visual Learning Guided Practice Independent Practice and Problem Solving Close/Assess and Differentiate lesson Quick Check 	 guided practice Do You Understand? question lesson Quick Check differentiated activities/worksheets leveled homework

Aligned to the 2014 Common Core Standards for Mathematics

ENGAGING STUDENTS • FOSTERING ACHIEVEMENT • CULTIVATING 21ST CENTURY GLOBAL SKILLS

the process in a vertical	b. prescribe differentiated instruction	
addition frame. (8-3)	c. assess leveled homework	
• will use place-value		
models and the standard algorithm to add two 2-		
digit numbers. (8-4)		
• will use the standard		
algorithm symbolically		
to add two-digit		
numbers with, and		
without, regrouping.		
(8-5)		
• will use number lines to		
model two-digit addition. (8-6)		
• will use paper and		
pencil to add three and		
four 2-digit numbers.		
(8-7)		
• will use different		
methods to help them		
solve addition problems.		
(8-8)		
 will draw pictures and write number sentences 		
to solve addition		
problems. (8-9)		

Differentiation

- TE pg. 211C
- embedded within each lesson
- differentiated worksheets/activities for each lesson
- · leveled homework for each lesson
- reteaching resources at the end of each lesson

Resources Provided

• enVision Math Common Core: Realize Edition Topic 5-11 teacher's guides, workbooks, digital resources, manipulatives

Topic 9

Aligned to the 2014 Common Core Standards for Mathematics

ENGAGING STUDENTS • FOSTERING ACHIEVEMENT • CULTIVATING 21ST CENTURY GLOBAL SKILLS

C	Content Area: Mathematics												
T	opic Title: Sul	btra	acting	Tw	o-Digit Numbers					Timefr	ame	: 1	4 days
	Lesson Components												
	21 st Century Themes												
	Global Awareness	X	Financial, Economic, Business, and Entrepreneurial Literacy			Civic Literacy			Health Literacy		Environmenta Literacy		
					<u>21st</u>	C	entury	Skil	ls				
	Creativity ar Innovation	nd		X	Critical Thinking and Problem Solving		d	X	Communication		y		Collaboration
I	nterdisciplina	ry (Conne	ecti	ons: Science, Soci	al S	Studies,	Read	ling,	Language Arts	S		
I	ntegration of T	Гес	hnolo	gy:	digital resources a	are	part of t	his s	eries				
N	Iaterials need	ed:											
	• connect	ing	cubes	S									
	 paper cl 	ips											
	 pencils 												
	 place va 			4									
	• number												
	• number cards 0-11												
	• colored pencils												
	• index cards												
	• tape												
T	opic 9 Vocabu	ılaı	ry:										

Goals/Objectives	Learning Activities/Instructional Strategies	Formative Assessment Tasks
Students: • will regroup 1 ten as 10 ones when subtracting. (9-1) • will use models to subtract a one-digit number from a two-digit number with or without regrouping. (9-2) • will subtract a one-digit number from a two-digit number with and without regrouping	 Lesson Sequence Interactive Math Story Topic Opener: game and vocabulary introduction Daily Common Core Review Problem-Based Interactive Learning Activity Develop the Concept: Visual Learning Guided Practice Independent Practice and Problem Solving Close/Assess and Differentiate 	 guided practice Do You Understand? question lesson Quick Check differentiated activities/worksheets leveled homework

no new vocabulary

Aligned to the 2014 Common Core Standards for Mathematics

ENGAGING STUDENTS • FOSTERING ACHIEVEMENT • CULTIVATING 21ST CENTURY GLOBAL SKILLS

using the standard	a.	lesson Quick Check	
algorithm. (9-3)	b.	prescribe differentiated instruction	
 will use models to 	c.	assess leveled homework	
subtract two-digits			
numbers, with and			
without regrouping.			
(9-4)			
 will use the standard 			
subtraction algorithm to			
subtract a two-digit			
number from another			
two-digit number. (9-5)			
• will use number lines to			
model two-digit			
subtraction. (9-6)			
 will relate addition to 			
subtraction by using one			
operation to check the			
other. (9-7)			
 will use different 			
methods to solve two-			
digit subtraction			
problems. (9-8)			
 will solve two-question 			
 _			

Differentiation

(9-9)

problems. They will select the operation to solve each question.

- TE pg. 253C
- embedded within each lesson
- differentiated worksheets/activities for each lesson
- leveled homework for each lesson
- reteaching resources at the end of each lesson

Resources Provided

• enVision Math Common Core: Realize Edition Topic 5-11 teacher's guides, workbooks, digital resources, manipulatives

Topic 10

Aligned to the 2014 Common Core Standards for Mathematics

ENGAGING STUDENTS • FOSTERING ACHIEVEMENT • CULTIVATING 21ST CENTURY GLOBAL SKILLS

(Content Area:	Ma	thema	atio	es								
1	Горіс Title: Pla	ісе	Value	to	1,000					Tir	nefrar	ne:	14 days
	Lesson Components												
	21 st Century Themes												
	Global Awareness	х	Financial, Economic, Business, and Entrepreneurial Literacy			Civic Literacy			Health Literacy			Environmental Literacy	
					21 st	C	entury	Skil	ls		•		
	Creativity an Innovation	nd		X	Critical Thinking Problem Solving		ıd	X	Con	nmunicatio	on	x	Collaboration
Ι	nterdisciplina	ry (Conne	cti	ons: Science, Soci	al S	Studies,	Reac	ling,	Language	Arts		
I	ntegration of	Гес	hnolo	gy:	digital resources a	are	part of t	his s	eries				
N	Materials need	ed:			-								
	• game m	ark	ers										
	 number 	cai	ds 10-	.99									
	 pencils 												
	 paper cl 	ips											
	 blank h 	und	reds c	har	rts								
	 place va 	ılue	block	S									
	 tape 												
	• stapler												
	 index ca 	ards	S										
	 number 	cul	be										
	• blank spinners												
1	Горіс 10 Vocab	ul	ary:										
	 hundred 	ls											
	• thousands												
	 expande 	ed f	orm										
	 standard 	d fo	rm										
	• number word												

Goals/Objectives	Learning Activities/Instructional Strategies	Formative Assessment Tasks
Students:	Lesson Sequence	• guided practice <i>Do You</i>
• will count by hundreds	1. Interactive Math Story	Understand? question
to 1,000. (10-1)	2. Topic Opener: game and vocabulary	• lesson Quick Check
• will use place-value	introduction	differentiated
models to show	3. Daily Common Core Review	activities/worksheets
numbers up to 1,000.	4. Problem-Based Interactive Learning	

compare

Aligned to the 2014 Common Core Standards for Mathematics

ENGAGING STUDENTS • FOSTERING ACHIEVEMENT • CULTIVATING 21ST CENTURY GLOBAL SKILLS

1	1	0-	7	١
((<i>)</i> –	Z)

- will identify and record three-digit numbers in expanded form, standard form, and number word form. (10-3)
- will add and subtract multiples of 10 or 100 to and from a three-digit number without regrouping. (10-4)
- will find, identify, and apply number patterns to numbers on a hundred chart. (10-5)
- will skip count by different amounts on the number line and use the patterns to identify the numbers that come next. (10-6)
- will compare three-digit numbers using the symbols <, >, and =. (10-7)
- will solve problems by finding number patterns. (10-8)

Activity

- 5. Develop the Concept: Visual Learning
 - a. Guided Practice
 - b. Independent Practice and Problem Solving
- 6. Close/Assess and Differentiate
 - a. lesson Quick Check
 - b. prescribe differentiated instruction
 - c. assess leveled homework

leveled homework

Differentiation

- TE pg. 295C
- embedded within each lesson
- differentiated worksheets/activities for each lesson
- leveled homework for each lesson
- reteaching resources at the end of each lesson

Resources Provided

• enVision Math Common Core: Realize Edition Topic 5-11 teacher's guides, workbooks, digital resources, manipulatives

Topic 11

Aligned to the 2014 Common Core Standards for Mathematics

ENGAGING STUDENTS • FOSTERING ACHIEVEMENT • CULTIVATING 21ST CENTURY GLOBAL SKILLS

Content Area: Mathematics						
Topic Title: Place Value	to 1,000		Time	frame: 14 days		
Lesson Components						
21st Century Themes						
Awareness Busin	ncial, Economic, ness, and epreneurial Literacy	Civic Literacy	Health Literacy	Environmental Literacy		
21st Century Skills						
Creativity and Innovation	x Critical Thinking Problem Solving	and x	Communication	x Collaboration		
Interdisciplinary Connec	ctions: Science, Socia	al Studies, Rea	ding, Language A	rts, Art		
Integration of Technolog	gy: digital resources an	re part of this	series			
Materials needed:						
• counters						
• pencils						
• paper	· a					
 place value blocks place value mat B 						
Topic 11 Vocabulary:	,					
• no new vocabular						

Goals/Objectives	Learning Activities/Instructional Strategies	Formative Assessment Tasks
 Students: will explore different strategies for adding three-digit numbers. (11-1) will add three-digit numbers mentally without regrouping. (11-2) will choose a method to see if the sum of two 3-digit numbers is enough to equal or exceed a given number. (11-3) will use place-value blocks to add two 3-digit numbers with regrouping. (11-4) will use paper and 	 Lesson Sequence Interactive Math Story Topic Opener: game and vocabulary introduction Daily Common Core Review Problem-Based Interactive Learning Activity Develop the Concept: Visual Learning Guided Practice Independent Practice and Problem Solving Close/Assess and Differentiate lesson Quick Check prescribe differentiated instruction assess leveled homework 	 guided practice Do You Understand? question lesson Quick Check differentiated activities/worksheets leveled homework

Aligned to the 2014 Common Core Standards for Mathematics

ENGAGING STUDENTS • FOSTERING ACHIEVEMENT • CULTIVATING 21ST CENTURY GLOBAL SKILLS

pencil to add two 3-digit		
numbers with		
regrouping. (11-5)		
 will explore different 		
strategies to subtract		
three-digit numbers.		
(11-6)		
• will be given a quantity		
and one of its parts, and		
then will find the		
missing part by		
counting on or counting		
back. (11-7)		
• will use estimation to		
select two numbers that		
have a given difference. (11-8)		
• will use models to		
subtract three-digit		
numbers with		
regrouping. (11-9)		
• will subtract three-digit		
numbers using a		
standard algorithm.		
(11-10)		
• will use logical		
reasoning to solve		
problems. (11-11)		
Differentiation		
• TE pg. 333C		
 embedded within each 1 	esson	
	ts/activities for each lesson	
 leveled homework for e 	ach jesson	

Resources Provided

reteaching resources at the end of each lesson

• enVision Math Common Core: Realize Edition Topic 5-11 teacher's guides, workbooks, digital resources, manipulatives

Aligned to the 2014 Common Core Standards for Mathematics

ENGAGING STUDENTS • FOSTERING ACHIEVEMENT • CULTIVATING 21ST CENTURY GLOBAL SKILLS

Unit 3 Overview

Content Area: Mathematics

Unit Title: Geometry

Target Course/Grade Level: Grade 2

Unit Summary

In this unit, children continue to explore both plane and solid (3D) figures with a focus on defining attributes (number of sides, number of angles). When given a defining attribute, students are asked to draw the appropriate figure. Students then partition rectangles into equal-sized squares and then count the squares to see how many fill the rectangle. This activity lays the groundwork for learning how to calculate area in grade 3. Students continue their explorations into partitioning rectangles and circles into equal pieces and describe the equal shares, and the whole in terms of the equal shares. Students learn that equal shares must have the same area, but do not have to have the same shape. They learn specific vocabulary words with which to describe the shares of the rectangle. These activities are the precursors to fraction work in grade 3; laying the groundwork for fraction understanding.

Primary interdisciplinary connections: Reading, Language Arts, Science, Social Studies

21st century themes:

- Critical Thinking/Problem Solving
- Communication
- Collaboration

Unit Rationale

Geometry connects mathematical understandings with real-world objects and applications.

Learning Targets

Standards

- <u>2.G.A.1</u> Recognize and draw shapes having specified attributes, such as a given number of angles or a given number of equal faces.¹ Identify triangles, quadrilaterals, pentagons, hexagons, and cubes.
- <u>2.G.A.2</u> Partition a rectangle into rows and columns of same-size squares and count to find the total number of them.
- <u>2.G.A.3</u> Partition circles and rectangles into two, three, or four equal shares, describe the shares using the words halves, thirds, half of, a third of, etc., and describe the whole as two halves, three thirds, four fourths. Recognize that equal shares of identical wholes need not have the same shape.

Content Statements

• Reason with shapes and their attributes.

	A
CPI#	Cumulative Progress Indicator (CPI) from NJDOE Model Curriculum
2.G.A.1	 Recognize and draw shapes having a given attribute (number of angles, number of equal faces). Identify triangles, quadrilaterals, pentagons, hexagons, and cubes.
2.G.A.2	Partition a rectangle into rows and columns of same-size squares and count to find the total number.
2.G.A.3	Partition circles and rectangles into two, three, or four equal shares.

¹ Sizes are compared directly or visually, not compared by measuring.

Aligned to the 2014 Common Core Standards for Mathematics

ENGAGING STUDENTS • FOSTERING ACHIEVEMENT • CULTIVATING 21ST CENTURY GLOBAL SKILLS

- Describe the shares using the words halves, thirds, half of, third of, etc.
- Describe the whole as two halves, three thirds, four fourths, etc.
- Recognize that equal shares of identical wholes do not have to have the same shape.

Unit Essential Questions

• Topic 12: How can shapes and solids be described, compared, and used to make other shapes?

Unit Enduring Understandings Topic 12:

- Three-dimensional or solid figures have length, width, and height. Many can be described, classified, and analyzed by their faces or flat surfaces, edges, and vertices. Many everyday objects closely approximate standard geometric solids.
- A shape can be identified by the number of its sides, vertices, or angles.
- Rectangles can be partitioned into equal shares.
- A region can be divided into equal-sized parts in different ways. Equal-sized parts of a region have the same area, but not necessarily the same shape.
- Some problems can be solved by reasoning about the conditions in the problem.

Unit Learning Targets

Students will be able to . .

- Recognize shapes having a given attribute.
- Draw shapes having a given attribute.
- Identify triangles, quadrilaterals, pentagons, hexagons, and cubes.
- Partition a rectangle into rows and columns of same size squares and count to find the total number.
- partition circles and rectangles in to two, three, or four equal shares.
- Use the words halves, thirds, half of, third of, to describe the equal shares.
- Describe the whole as two halves, three thirds, four fourths, etc.
- Recognize that equal shares do not have to have the same shape.

Evidence of Learning

Summative Assessment (14 days per topic)

Each topic has a summative test and performance assessment.

Materials needed: listed in each topic as per teacher's guide for that topic.

Teacher Resources:

enVision Math Common Core: Realize Edition Topic 12, Geometry

Formative Assessments

• teacher observation

• prior knowledge assessment

homework

· guided practice

Aligned to the 2014 Common Core Standards for Mathematics

ENGAGING STUDENTS • FOSTERING ACHIEVEMENT • CULTIVATING 21ST CENTURY GLOBAL SKILLS

• Lesson Additional Activity

- Lesson Quick Check
- Daily Common Core Review

Topic/Lesson Plans									
Topic	Timeframe								
Topic 12 Geometry	14 days								

Teacher Notes:

This unit consists of 1 topic from the *enVision Math Common Core* series with seven lessons in the topic. This topic addresses the Geometry domain of the Common Core Standards for Mathematics for Grade 2 students. In addition, this topic addresses all eight of the Standards for Mathematical Practice.

Essential questions and enduring understandings were taken directly from the textbook series used by the district, *enVision Math Common Core: Realize Edition*

Curriculum Development Resources

Click the links below to access additional resources used to design this unit:

NJDOE. "Model Curriculum: Mathematics (K-12) - Grade 2." *Model Curriculum: Mathematics (K-12) - Grade 2*. New Jersey Dept. of Education, n.d. Web. 08 Apr. 2015. http://www.state.nj.us/education/modelcurriculum/math/1.shtml.

Charles, Randall. *enVision Math Common Core*. Realize ed. Grade 1. Upper Saddle River: Pearson Education, 2015. Print. enVision Math Common Core

"Grade 2 » Geometry » Geometry. N.p., n.d. Web. 10 Apr. 2015. http://www.corestandards.org/Math/Content/1/OA/

Common Core Standards Writing Team. (2011, May 29). Progressions for the Common Core State Standards in Mathematics (draft). *K, Counting and Cardinality; K–5, Operations and Algebraic Thinking.* Tucson, AZ: Institute for Mathematics and Education, University of Arizona.

	Topic 12										
Co	Content Area: Mathematics										
To	Topic Title: Geometry Timeframe: 14 days										
			Less	on	Components	s					
			<u>21st (</u>	Cei	ntury Theme	es					
Global x Financial, Economic, Business, and Entrepreneurial Literacy					Civic Literacy		Health Literacy		Environmental Literacy		

Aligned to the 2014 Common Core Standards for Mathematics
ENGAGING STUDENTS • FOSTERING ACHIEVEMENT • CULTIVATING 21ST CENTURY GLOBAL SKILLS

	21st Century Skills											
	Creativity and	X	Critical Thir		X	Communication	X	Collaboration				
	Innovation		Problem Sol									
	Interdisciplinary Connections: Science, Social Studies, Reading, Language Arts, Art											
In	Integration of Technology: digital resources are part of this series											
M	aterials needed:											
•	counters											
•	paper clips											
•	pencils											
•	geometric solids											
•	clay											
•	straws											
•	pipe cleaners											
•	crayons											
•	construction paper											
•	markers											
•	rulers											
•	color tiles											
•	sticky notes											
To	pic 12 Vocabulary:											
	 sphere 											
	 pyramid 											
	 cylinder 											
	• cone											
	• cube											
	 rectangular prism 	1										
	 solid figure 											
	 flat surface 											
	• face											
	• edge											
	• vertex (vertices)											
	• plane shapes											
	• circle											
	• square											
	• triangle											
	• rectangle											
	• polygon											
	• angle											
	• side											

quadrilateral

Aligned to the 2014 Common Core Standards for Mathematics

ENGAGING STUDENTS • FOSTERING ACHIEVEMENT • CULTIVATING 21ST CENTURY GLOBAL SKILLS

- pentagon
- hexagon
- · rows columns

Goals/Objectives	Learning Activities/Instructional Strategies	Formative Assessment Tasks
 Students: will identify solid figures by their faces or flat surfaces, edges, and vertices. (12-1) will identify the plane shapes that form the flat surfaces of solid figures. (12-2) will identify and draw polygons (triangles, quadrilaterals, pentagons, and hexagons) and list their attributes. (12-3) will determine whether a shape has been divided into equal or unequal parts. If the parts are equal, children will count the parts. (12-4) will divide rectangles into equal squares and count how many squares are needed to completely partition the rectangle. (12-5) will divide rectangles into equal shares with different shapes. (12-6) will use clued to solve riddles about plane shapes and solid figures. (12-7) Differentiation 	 Interactive Math Story Topic Opener: game and vocabulary introduction Daily Common Core Review Problem-Based Interactive Learning Activity Develop the Concept: Visual Learning Guided Practice Independent Practice and Problem Solving Close/Assess and Differentiate lesson Quick Check prescribe differentiated instruction assess leveled homework 	 guided practice Do You Understand? question lesson Quick Check differentiated activities/worksheets leveled homework

Differentiation

• TE pg. 383C

Aligned to the 2014 Common Core Standards for Mathematics

ENGAGING STUDENTS • FOSTERING ACHIEVEMENT • CULTIVATING 21ST CENTURY GLOBAL SKILLS

- embedded within each lesson
- differentiated worksheets/activities for each lesson
- leveled homework for each lesson
- reteaching resources at the end of each lesson

Resources Provided

• *enVision Math Common Core: Realize Edition* Topic 12 teacher's guide, workbooks, digital resources, manipulatives

Unit 4 Overview

Content Area: Mathematics

Unit Title: Measurement and Data

Target Course/Grade Level: Grade 2

Unit Summary

In this unit students learn the to identify the different coins that make up our monetary system, and the value of those coins. They learn to represent varying amounts of money using coin combinations and dollar bills as well as represent money amounts in writing. When writing money amounts students are taught how to correctly use the \$ and $$\phi$$ symbols and the decimal point. Students solve problems involving two-digit money amounts, applying the addition and subtraction strategies they have learned to add and subtract whole numbers.

The measurement focus in this unit is on measuring length and height using nonstandard and standard units. Students learn to measure to the nearest whole unit using inch rulers, centimeter rulers, yardsticks and meter sticks. They learn to record these measurements to the nearest inch, foot, yard, centimeter, or meter depending upon the measuring tool used.

Students learn to take measurement data and record it on a line plot. Students continue work with pictographs and bar graphs to represent categorical data. In addition, this unit teaches students to tell time to five minutes and record time using A.M. and P.M.

Primary interdisciplinary connections: Reading, Language Arts, Science, Social Studies

21st century themes:

- Critical Thinking/Problem Solving
- Communication
- Collaboration

Unit Rationale

Geometric measurement connects the two most critical domains of early mathematics, geometry and number, with each providing conceptual support to the other. Measurement is central to mathematics, to other areas of mathematics (e.g., laying a sensory and conceptual foundation for arithmetic with fractions).

Aligned to the 2014 Common Core Standards for Mathematics

ENGAGING STUDENTS • FOSTERING ACHIEVEMENT • CULTIVATING 21ST CENTURY GLOBAL SKILLS

to other subject matter domains, especially science, and to activities in everyday life. For these reasons, measurement is a core component of the mathematics curriculum. (Common Core Standards Writing Team, 2012)

As students work with data in Grades K–5, they build foundations for their study of statistics and probability in Grades 6 and beyond, and they strengthen and apply what they are learning in arithmetic. (Common Core Standards Writing Team, 2011)

Learning Targets

Standards

- <u>2.MD.A.1</u> Measure the length of an object by selecting and using appropriate tools such as rulers, yardsticks, meter sticks, and measuring tapes.
- <u>2.MD.A.2</u> Measure the length of an object twice, using length units of different lengths for the two measurements; describe how the two measurements relate to the size of the unit chosen.
- 2.MD.A.3 Estimate lengths using units of inches, feet, centimeters, and meters.
- <u>2.MD.A.4</u> Measure to determine how much longer one object is than another, expressing the length difference in terms of a standard length unit.
- <u>2.MD.B.5</u> Use addition and subtraction within 100 to solve word problems involving lengths that are given in the same units, e.g., by using drawings (such as drawings of rulers) and equations with a symbol for the unknown number to represent the problem.
- <u>2.MD.C.7</u> Tell and write time from analog and digital clocks to the nearest five minutes, using a.m. and p.m.
- <u>2.MD.C.8</u> Solve word problems involving dollar bills, quarters, dimes, nickels, and pennies, using \$ and ¢ symbols appropriately. Example: If you have 2 dimes and 3 pennies, how many cents do you have?
- <u>2.MD.D.9</u> Generate measurement data by measuring lengths of several objects to the nearest whole unit, or by making repeated measurements of the same object. Show the measurements by making a line plot, where the horizontal scale is marked off in whole-number units.
- <u>2.MD.D.10</u> Draw a picture graph and a bar graph (with single-unit scale) to represent a data set with up to four categories. Solve simple put-together, take-apart, and compare problems using information presented in a bar graph.
- 2.NBT.A.2 Count within 1000; skip-count by 5s, 10s, and 100s.
- <u>2.NBT.B.5</u> Fluently add and subtract within 100 using strategies based on place value, properties of operations, and/or the relationship between addition and subtraction.
- <u>2.NBT.B.9</u> Explain why addition and subtraction strategies work, using place value and the properties of operations.

Content Statements

- Measure and estimate lengths in standard units.
- Relate addition and subtraction to length.
- Work with time and money.
- Represent and interpret data.
- Use place value understanding and properties of operations to add and subtract.
- Understand place value.

CPI#	Cumulative Progress Indicator (CPI) from NJDOE Model Curriculum
2.MD.A.1	Estimate or measure length using appropriate tools (inches, feet, centimeters, meters).

Aligned to the 2014 Common Core Standards for Mathematics

ENGAGING STUDENTS • FOSTERING ACHIEVEMENT • CULTIVATING 21ST CENTURY GLOBAL SKILLS

2.MD.A.2/A.3	Measure and object with two different units of measure (within the same system) and explain that the difference in results is due to the size of the unit of measure.
2.MD.A.4	Compare the lengths of two objects using the same unit of measure and determine which one is longer.
2.MD.B.5	Add and subtract within 100 in word problems involving lengths using a symbol to represent the unknown number.
2.MD.C.7	Tell and write time using analog and digital clocks to the nearest 5 minutes using A.M. and P.M.
2.MD.C.8	Identify, recognize, and solve word problems with dollar bills, quarters, dimes, nickels, and pennies using the \$ and the ¢ symbols appropriately.
2.MD.D.9	Use tools of measurement to measure lengths of several objects to the nearest whole inch; represent this data on a line plot with appropriate whole number units on the horizontal scale.
2.MD.D.10	Draw a picture graph or bar graph with up to four categories; solve simple put-together, take-apart and compare problems based on information in the graph.
2.NBT.A.2	Skip count by 1s, 5s and 10s to 1000 beginning at any multiple of 5.
2.NBT.B.5	Use a variety of strategies to add and subtract within 100.
2.NBT.B.9	Apply addition and subtraction strategies based on place value and properties of operations and explain why they work using drawings or objects.

Unit Essential Questions

- Topic 13: What strategies can be used to count money?
- Topic 14: How can sums and differences be estimated?
- Topic 15: What is the process for measuring length?
- Topic 16: How can clocks, bar graphs, and pictographs be used to show data and answer questions?

Unit Enduring Understandings Topic 13:

- Specific coins or bills each have a unique value. The size of a coin does not indicate its value.
- Money amounts can usually be counted in different ways. When counting money, it is usually easier to start with the coin or bill with the greatest value.
- The same amount of money can often be represented using different combinations of coins and bills.
- Some problems can be solved by generating a list of outcomes and organizing that list in a systematic way so all outcomes are accounted for.

Topic 14:

- The process for adding money, written using cent notation, is the same as adding whole numbers.
- The process for subtracting money, written using cent notation, is the same as subtracting whole numbers.
- Rounding can be used to estimate sums and differences as can place value and number relationships.

Aligned to the 2014 Common Core Standards for Mathematics

ENGAGING STUDENTS • FOSTERING ACHIEVEMENT • CULTIVATING 21ST CENTURY GLOBAL SKILLS

• Some problems can be solved by making a reasoned first try for what the answer might be, and then through additional reasoning arrive at the correct answer.

Topic 15:

- The length of some objects is measurable.
- The length of any object can be used as a measurement unit for length, but a standard unit, such as an inch or centimeter, is always the same length.
- The length of any object can be used as a measurement unit for length, but a standard unit is always the same length.
- Measurement is a process of comparing a uit to the object being measured. The length of any object can be used as a measurement unit for length.
- Measurements in the same unit such as inches, can be added or subtracted in the same way as adding and subtracting whole numbers. The measurement unit needs to be written with the sum or difference.
- The length of any two objects can be compared by subtracting to find the difference.
- Some problems can be solved by using objects to act out the actions in the problem.

Topic 16:

- Time can be given to the nearest five minutes. Time can be expressed using different units that are related to each other. A.M. and P.M. are used to designate certain time periods.
- Time can be expressed as before or after the hour.
- A calendar shows days, weeks, and months.
- That same time can be stated and written in more than one way.
- Data can be organized in different ways.
- The lengths of objects can be organized in different ways. A line plot can be used as a visual representation of the relative lengths of object.
- Each type of graph is most appropriate for certain kinds of data. Pictographs and bar graphs make it easy to compare data.
- Some problems can be solved by making,

Aligned to the 2014 Common Core Standards for Mathematics

ENGAGING STUDENTS • FOSTERING ACHIEVEMENT • CULTIVATING 21ST CENTURY GLOBAL SKILLS

reading, and analyzing a graph.

Unit Learning Targets

Students will be able to . .

- estimate lengths of objects
- measure lengths of objects using appropriate tools
- measure in inches, centimeters, feet, and meters
- compare measurements of an object taken with two different units of measure (within the same measurement system) and explain that the difference is due to the size of the unit chosen (there will be more inches than feet for the length of a given object because more of the smaller unit is needed)
- compare lengths of two objects measured with the same unit and determine how much longer one object is than the other.
- Add and subtract within 100 to find the solution to word problems involving length using a symbol to represent the unknown quantity.
- use a number line to find sums and differences related to length using equally spaced points on the number line.
- tell and write time using analog and digital clocks to the nearest five minutes using A.M. and P.M. notation.
- solve word problems involving dollar bills, quarters, dimes, nickels and pennies using the \$ and ¢ symbols appropriately.
- use tools of measurement to measure objects to the nearest whole unit.
- represent measurements of several objects to the nearest whole unit on a line plot with appropriate whole number units on the horizontal scale.
- draw a picture graph and bar graph with a single unit scale and up to four categories.
- solve simple put-together, take-apart, and compare problems using information represented in the graph.
- count within 1000 by ones, fives, tens and hundreds.
- choose a strategy (place value, properties of operations, inverse relationship) to add and subtract within 100.
- apply addition and subtraction strategies based on place value and properties of operations and explain why they work using drawings or objects.

Evidence of Learning

Summative Assessment (14 days per topic)

Each topic has a summative test and performance assessment.

Materials needed: listed in each topic as per teacher's guide for that topic.

Teacher Resources:

enVision Math Common Core: Realize Edition Topic 13, Counting Money

enVision Math Common Core: Realize Edition Topic 14, Money

enVision Math Common Core: Realize Edition Topic 15, Measuring Length

enVision Math Common Core: Realize Edition Topic 16, Time, Graphs, and Data

Formative Assessments

teacher observation

prior knowledge assessment

homework

guided practice

Aligned to the 2014 Common Core Standards for Mathematics

ENGAGING STUDENTS • FOSTERING ACHIEVEMENT • CULTIVATING 21ST CENTURY GLOBAL SKILLS

• Lesson Additional Activity

- Lesson Quick Check
- Daily Common Core Review

Topic/Lesson Plans								
Topic Timeframe								
Topic 13 Counting Money	14 days							
Topic 14 Money	14 days							
Topic 15 Measuring Length	14 days							
Topic 16 Time, Graphs, and Data	14 days							

Teacher Notes:

This unit consists of 4 topics from the *enVision Math Common Core* series with anywhere from four to nine lessons in each topic. This four topics address the Measurement and Data domain of the Common Core Standards for Mathematics for Grade 2 students. In addition, these topics address all eight of the Standards for Mathematical Practice.

Essential questions and enduring understandings were taken directly from the textbook series used by the district, enVision Math Common Core: Realize Edition

Curriculum Development Resources

Click the links below to access additional resources used to design this unit:

NJDOE. "Model Curriculum: Mathematics (K-12) - Grade 2." *Model Curriculum: Mathematics (K-12) - Grade 2*. New Jersey Dept. of Education, n.d. Web. 08 Apr. 2015. http://www.state.nj.us/education/modelcurriculum/math/1.shtml.

Charles, Randall. *enVision Math Common Core*. Realize ed. Grade 1. Upper Saddle River: Pearson Education, 2015. Print. enVision Math Common Core

"Grade 2 » Measurement and Data » Measurement and Data. N.p., n.d. Web. 10 Apr. 2015. http://www.corestandards.org/Math/Content/1/OA/

Common Core Standards Writing Team. (2011, June 20). K-3, Categorical Data;

Grades 2–5, Measurement Data (draft). *K–3, Categorical Data; Grades 2–5, Measurement Data*. Tucson, AZ: Institute for Mathematics and Education, University of Arizona.

Common Core Standards Writing Team. (2012, June 23). *K*–5, *Geometric Measurement* (draft). *K*–5, *Geometric Measurement*. Tucson, AZ: Institute for Mathematics and Education, University of Arizona

Topic 13								
Content Area: Mathematics								
Topic Title: Counting Money	Timeframe: 14 days							

Aligned to the 2014 Common Core Standards for Mathematics

ENGAGING STUDENTS • FOSTERING ACHIEVEMENT • CULTIVATING 21ST CENTURY GLOBAL SKILLS

Lesson Components											
21st Century Themes											
Global x Financial, Economic, Business, and Entrepreneurial Literacy Entrepreneurial Literacy Entrepreneurial Literacy											
21 st Century Skills											
Creativity and Innovation x Critical Thinking and Problem Solving x Communication x Collaboration											
Interdisciplinary Connections: Science, Social Studies, Reading, Language Arts,											
Integration of Technology: digital resources are part of this series											
Materials needed: • game markers • coins • paper clips • pencils • paper bag • number cube • dollar bills Topic 13 Vocabulary: • half dollar • quarter • dime • nickel • penny • coins • cents (\$\phi\$) • greatest value • least value • dollar bill • dollar coin											
dollar sign degimel point											
decimal point											

Goals/Objectives	Learning Activities/Instructional Strategies	Formative Assessment Tasks
Students:	Lesson Sequence	• guided practice Do You
• will identify the value	1. Interactive Math Story	Understand? question
of a group of half-		

tally mark

Aligned to the 2014 Common Core Standards for Mathematics

ENGAGING STUDENTS • FOSTERING ACHIEVEMENT • CULTIVATING 21ST CENTURY GLOBAL SKILLS

- dollars, quarters, dimes, nickels, and pennies. (13-1)
- will count collections of coins that include halfdollars, quarters, dimes, nickels, and pennies.
 (13-2)
- will show the same amount of money using different sets of coins. (13-3)
- will count money amounts greater than one dollar and write the amount with a dollar sign and a decimal point. (13-4)
- will make an organized list to find different combinations of coins. (13-5)

- 2. Topic Opener: game and vocabulary introduction
- 3. Daily Common Core Review
- 4. Problem-Based Interactive Learning Activity
- 5. Develop the Concept: Visual Learning
 - a. Guided Practice
 - b. Independent Practice and Problem Solving
- 6. Close/Assess and Differentiate
 - a. lesson Quick Check
 - b. prescribe differentiated instruction
 - c. assess leveled homework

- lesson Quick Check
- differentiated activities/worksheets
- leveled homework

Differentiation

- TE pg. 417C
- embedded within each lesson
- differentiated worksheets/activities for each lesson
- leveled homework for each lesson
- reteaching resources at the end of each lesson

Resources Provided

• *enVision Math Common Core: Realize Edition* Topic 13 teacher's guide, workbooks, digital resources, manipulatives

Topic 14	
Content Area: Mathematics	
Topic Title: Money	Timeframe: 14 days

Aligned to the 2014 Common Core Standards for Mathematics

ENGAGING STUDENTS • FOSTERING ACHIEVEMENT • CULTIVATING 21ST CENTURY GLOBAL SKILLS

	Lesson Components												
	21st Century Themes												
	Global x Financial, Economic, Business, and Entrepreneurial Literacy					Civic Literacy			Health Literacy		Environmental Literacy		
	21st Century Skills												
Creativity and x Critical Thinking Innovation Problem Solving						and x		Communication			X	Collaboration	
Iı	nterdisciplina	ry (Conne	cti	ons: Science, Soci	al S	Studies,	Rea	ding,	Language Arts	s,		
Iı	ntegration of T	Гес	hnolog	gy:	digital resources a	are	part of t	his s	series				
N	laterials need	ed:											
	• counters	3											
	coins												
	• connect	ing	cubes										
T	opic 14 Vocab	ula	ary:										
	 no new vocabulary 												

Goals/Objectives	Learning Activities/Instructional Strategies	Formative Assessment Tasks
 Students: will complete and record addition problems using two-digit coin amounts. (14-1) will subtract using two-digit coin amounts. (14-2) will estimate the sum and difference of two 2-digit numbers. (14-3) will solve problems involving adding and subtracting money by using the try, check, and revise method. (14-4) 	 Lesson Sequence Interactive Math Story Topic Opener: game and vocabulary introduction Daily Common Core Review Problem-Based Interactive Learning Activity Develop the Concept: Visual Learning Guided Practice Independent Practice and Problem Solving Close/Assess and Differentiate lesson Quick Check prescribe differentiated instruction assess leveled homework 	 guided practice Do You Understand? question lesson Quick Check differentiated activities/worksheets leveled homework
Differentiation		

Aligned to the 2014 Common Core Standards for Mathematics

ENGAGING STUDENTS • FOSTERING ACHIEVEMENT • CULTIVATING 21ST CENTURY GLOBAL SKILLS

- TE pg. 443C
- embedded within each lesson
- differentiated worksheets/activities for each lesson
- leveled homework for each lesson
- reteaching resources at the end of each lesson

Resources Provided

• *enVision Math Common Core: Realize Edition* Topic 14 teacher's guide, workbooks, digital resources, manipulatives

Topic 15										
Content Area: Mathem	atio	es								
Topic Title: Money Timeframe: 14 days										
		Lesso	on	Compo	nen	ts				
21st Century Themes										
Awareness Bus	nes	l, Economic, , and neurial Literacy		Civic Literacy			Health Literacy		Environmental Literacy	
21st Century Skills										
Creativity and x Critical Thinking and x Com Innovation Problem Solving x Com		nmunication	·	X	Collaboration					
Interdisciplinary Connections: Science, Social Studies, Reading, Language Arts,										
Integration of Technology: digital resources are part of this series										

Aligned to the 2014 Common Core Standards for Mathematics

ENGAGING STUDENTS • FOSTERING ACHIEVEMENT • CULTIVATING 21ST CENTURY GLOBAL SKILLS

Materials needed:

- counters
- connecting cubes
- number cube
- pencils
- small paper clips
- crayons
- erasers
- · index cards
- rulers (standard)
- centimeter rulers
- yardsticks
- metersticks
- large paper clips
- crayons
- staplers
- books
- string

Topic 15 Vocabulary:

- unit
- length
- inch (in.)
- width
- height
- nearest inch
- centimeter (cm)
- nearest centimeter
- foot (ft)
- yard (yd)
- meter (m)

Goals/Objectives	Learning Activities/Instructional Strategies	Formative Assessment Tasks
Students: • will measure the	Lesson Sequence 1. Interactive Math Story	• guided practice <i>Do You Understand?</i> question
lengths of objects using nonstandard units. (15-1)	 Topic Opener: game and vocabulary introduction Daily Common Core Review 	 lesson Quick Check differentiated activities/worksheets
• will estimate and measure items using	4. Problem-Based Interactive Learning Activity	leveled homework

Aligned to the 2014 Common Core Standards for Mathematics

ENGAGING STUDENTS • FOSTERING ACHIEVEMENT • CULTIVATING 21ST CENTURY GLOBAL SKILLS

inches. (15-2)

- will estimate and measure length and height using centimeters. (15-3)
- will estimate and measure items that about an inch, foot, and yard. (15-4)
- will estimate and measure the lengths and heights of objects in centimeters and meters. (15-5)
- will estimate and measure the lengths and heights of objects using different units. (15-6)
- will use addition and subtraction to solve measurement problems. (15-7)
- will measure to compare length and express the length difference in a standard length unit. (15-8)
- will use string and rulers to measure to the nearest inch the length of paths that are not straight. (15-9)

- 5. Develop the Concept: Visual Learning
 - a. Guided Practice
 - b. Independent Practice and Problem Solving
- 6. Close/Assess and Differentiate
 - a. lesson Quick Check
 - b. prescribe differentiated instruction
 - c. assess leveled homework

Differentiation

- TE pg. 465C
- embedded within each lesson
- differentiated worksheets/activities for each lesson
- leveled homework for each lesson
- reteaching resources at the end of each lesson

Resources Provided

• *enVision Math Common Core: Realize Edition* Topic 15 teacher's guide, workbooks, digital resources, manipulatives

Aligned to the 2014 Common Core Standards for Mathematics

ENGAGING STUDENTS • FOSTERING ACHIEVEMENT • CULTIVATING 21ST CENTURY GLOBAL SKILLS

						-	Topic 16	=					
	~						opic 10)					
	Content Area: Mathematics												
1	Topic Title: Tit	me,	Grapi	hs,	and Data					Timefi	ram	ie:	4 days
					Less	on	Compo	oner	nts				
					21 st	Cei	ntury T	hen	nes				
	Global x Financial, Economic, Awareness Business, and Entrepreneurial Literacy Entrepreneurial Literacy Entrepreneurial Literacy												
					21 st	C	entury	Skil	lls				
	Creativity an Innovation	nd		X	Critical Thinking Problem Solving		d	X	Cor	nmunication		X	Collaboration
I	nterdisciplinaı	ry (Conne	cti	ons: Science, Soci	al S	Studies,	Read	ding,	Language Arts	s,		
Ι	ntegration of T	Гес	hnolog	gy:	digital resources a	are	part of t	his s	eries				
N	Materials need	ed:											
	• counters	S											
	 pencils 												
	 paper cl 	ips											
	 clock fa 	ce											
	• geared d	len	onstra	tio	n clock								
	• student	sci	ssors										
	• index cards												
	• inch ruler												
	• cups												
	• connecting cubes												
	 unit cub 	es											
	• two-color counters												
1	Topic 16 Vocab	ul	ary:										
	 minute l 	han	d										
	• minute												
	 hour har 	nd											
	• hour												
	 half hou 	ır											
	• A.M.												
	• P.M.												
	• quarter	pas	t										
	• half pas	t											
	• quarter 1	to											

Aligned to the 2014 Common Core Standards for Mathematics

ENGAGING STUDENTS • FOSTERING ACHIEVEMENT • CULTIVATING 21ST CENTURY GLOBAL SKILLS

- bar graph
- data
- line plot
- symbol
- pictograph

Goals/Objectives	Learning Activities/Instructional Strategies	Formative Assessment Tasks
 will learn to associate numerals on an analog clock face with increments of five minutes. (16-1) will read and express time in terms of quarter and half past an hour and before an hour. (16-2) will represent a set of data in a bar graph and use the bar graph to solve problems. (16-3) will use rulers to measure objects and graph the results. (16-4) will make and use a pictograph to solve problems. (16-5) will use picture graphs and bar graphs to solve problems. (16-6) 	 Lesson Sequence Interactive Math Story Topic Opener: game and vocabulary introduction Daily Common Core Review Problem-Based Interactive Learning Activity Develop the Concept: Visual Learning Guided Practice Independent Practice and Problem Solving Close/Assess and Differentiate lesson Quick Check prescribe differentiated instruction assess leveled homework 	 guided practice Do You Understand? question lesson Quick Check differentiated activities/worksheets leveled homework

Differentiation

- TE pg. 507C
- embedded within each lesson
- differentiated worksheets/activities for each lesson
- leveled homework for each lesson
- reteaching resources at the end of each lesson

Resources Provided

Aligned to the 2014 Common Core Standards for Mathematics

ENGAGING STUDENTS • FOSTERING ACHIEVEMENT • CULTIVATING 21ST CENTURY GLOBAL SKILLS

• *enVision Math Common Core: Realize Edition* Topic 16 teacher's guide, workbooks, digital resources, manipulatives

LESSON REFLECTION

Reflect on the lesson you have developed and rate the degree to which the lesson *Strongly*, *Moderately* or *Weakly* meets the criteria below.

Lesson Activities:	Strongly	Moderately	Weakly
Are challenging and require higher order thinking and problem solving skills			
Allow for student choice			
Provide scaffolding for acquiring targeted knowledge/skills			
Integrate global perspectives			
Integrate 21 st century skills			
Provide opportunities for interdisciplinary connection and transfer of knowledge and skills			
Foster student use of technology as a tool to develop critical thinking, creativity and innovation skills			
Are varied to address different student learning styles and preferences			
Are differentiated based on student needs			
Are student-centered with teacher acting as a facilitator and co-learner during the teaching and learning process			
Provide means for students to demonstrate knowledge and skills and progress in meeting learning goals and objectives			
Provide opportunities for student reflection and self-assessment			

Aligned to the 2014 Common Core Standards for Mathematics

ENGAGING STUDENTS • FOSTERING ACHIEVEMENT • CULTIVATING 21ST CENTURY GLOBAL SKILLS

Provide data to inform and adjust instruction to better meet		
the varying needs of learners		

	Curriculum Design Template				
Co	Content Area:				
Course Title: Grade Level:		Grade Level:			
	Unit Plan 1	Pacing Guide			
	Unit Plan 1	Pacing Guide			
	Unit Plan 3	Pacing Guide			
	Unit Plan 4	Pacing Guide			
	Unit Plan 5	Pacing Guide			
	Unit Plan 6	Pacing Guide			

Created for New Jersey school districts through a project of the New Jersey Department of Education, Office of Academic Standards, in partnership with the N.J. Association for Supervision and Curriculum Development and the N.J. Principals and Supervisors Association.

Aligned to the 2014 Common Core Standards for Mathematics

ENGAGING STUDENTS • FOSTERING ACHIEVEMENT • CULTIVATING 21ST CENTURY GLOBAL SKILLS

Date Created:
Board Approved on: